Tutorial K-Map

a) Use K-Map to find the minimum SOP from each expression:

1. $X = \overline{A}\overline{B}\overline{C} + \overline{A}\overline{B}C + A\overline{B}C$
2. $X = AC\left(\overline{B} + C\right)$
3. $X = \overline{A}\left(BC + B\overline{C}\right) + A\left(BC + B\overline{C}\right)$
4. $X = \overline{A}\overline{B}\overline{C} + A\overline{B}\overline{C} + \overline{A}B\overline{C} + AB\overline{C}$

b) Use the Karnaugh Map method; find the minimum SOP expression in the truth table below:

A	B	C	f
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	1

(a)

A	B	C	f
0	0	0	1
0	0	1	1
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	1
1	1	0	0
1	1	1	0

(b)

A	B	C	f
0	0	0	1
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	1

(c)

A	B	C	f
0	0	0	1
0	0	1	1
0	1	0	1
0	1	1	1
1	0	0	1
1	0	1	1
1	1	0	1
1	1	1	1

(d)

A	B	C	F1	F2
0	0	0	1	0
0	0	1	1	0
0	1	0	0	1
0	1	1	0	1
1	0	0	0	1
1	0	1	0	1
1	1	0	1	0
1	1	1	1	0

(e)

A	B	C	F1	F2
0	0	0	1	0
0	0	1	1	0
0	1	0	0	1
0	1	1	0	1
1	0	0	1	0
1	0	1	1	0
1	1	0	0	1
1	1	1	0	1

(f)

A	B	C	D	X
0	0	0	0	1
0	0	0	1	1
0	0	1	0	0
0	0	1	1	1
0	1	0	0	0
0	1	0	1	1
0	1	1	0	1
0	1	1	1	0
1	0	0	0	0
1	0	0	1	1
1	0	1	0	0
1	0	1	1	0
1	1	0	0	1
1	1	0	1	0
1	1	1	0	0
1	1	1	1	0

(g)

A	B	C	D	X
0	0	0	0	0
0	0	0	1	0
0	0	1	0	1
0	0	1	1	0
0	1	0	0	1
0	1	0	1	1
0	1	1	0	0
0	1	1	1	1
1	0	0	0	0
1	0	0	1	0
1	0	1	0	0
1	0	1	1	1
1	1	0	0	1
1	1	0	1	0
1	1	1	0	0
1	1	1	1	1

(h)

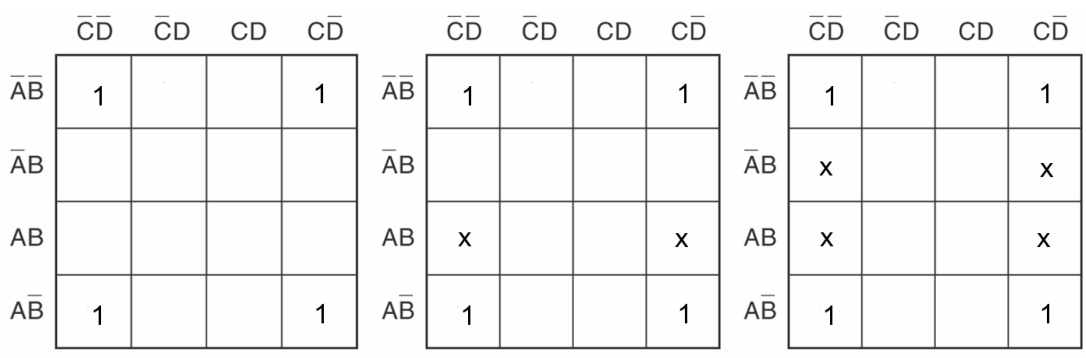
A	B	C	D	X
0	0	0	0	0
0	0	0	1	1
0	0	1	0	1
0	0	1	1	0
0	1	0	0	0
0	1	0	1	1
0	1	1	0	1
0	1	1	1	1
1	0	0	0	1
1	0	0	1	0
1	0	1	0	1
1	0	1	1	0
1	1	0	0	1
1	1	0	1	1
1	1	1	0	0
1	1	1	1	1

(i)

A	B	C	D	X
0	0	0	0	1
0	0	0	1	1
0	0	1	0	1
0	0	1	1	1
0	1	0	0	1
0	1	0	1	1
0	1	1	0	1
0	1	1	1	1
1	0	0	0	1
1	0	0	1	1
1	0	1	0	1
1	0	1	1	1
1	1	0	0	1
1	1	0	1	1
1	1	1	0	1
1	1	1	1	1

(j)

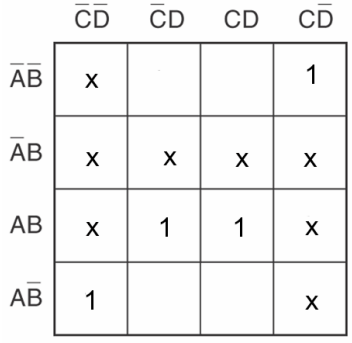
c) Use K-Map to find the minimum SOP from:



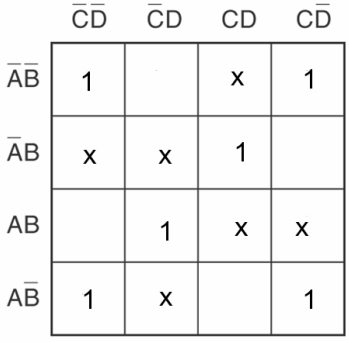
(a)

(b)

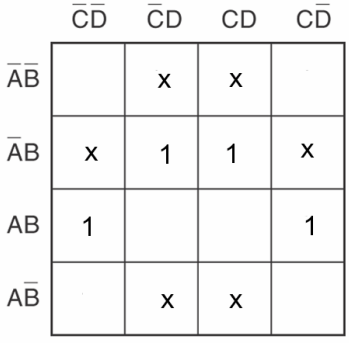
(c)



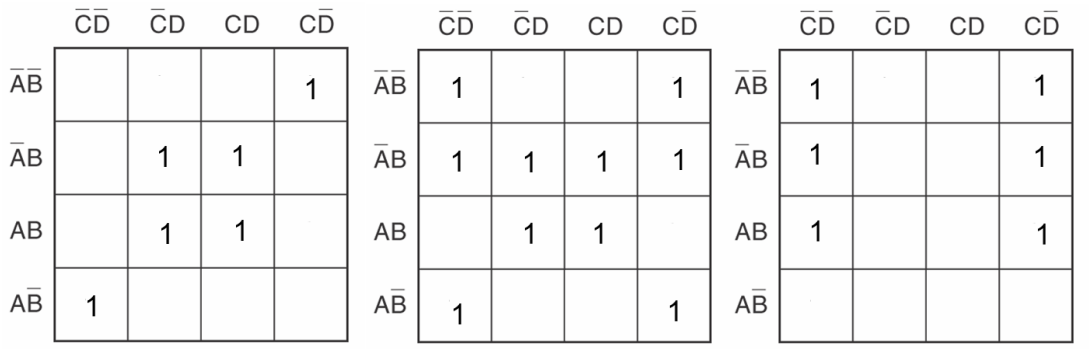
(d)



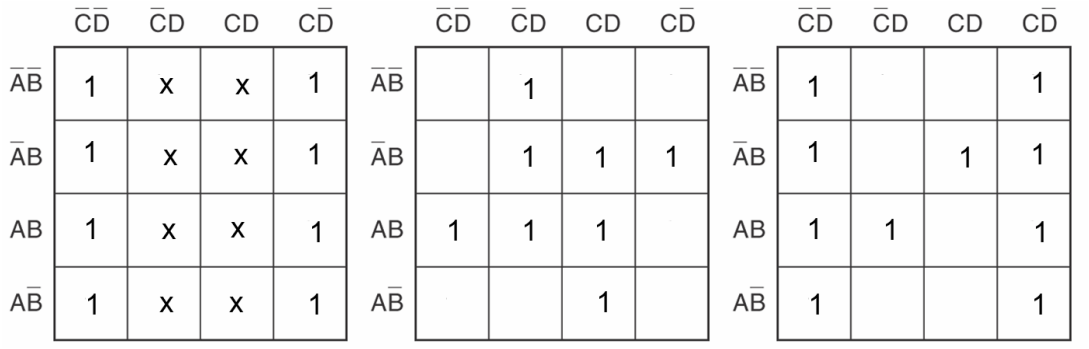
(e)



(f)



(g) (h) (i)



(j) (k) (l)

d) A family consists of Father (F), Mother (M), Son (S) and Daughter (D). They want to build a voting machine according to the following rules. An output (X) is carried if:

- Both Father and Mother vote YES
- Father, Mother and anyone of the children vote YES
- Mother and both children vote YES
- Father and both children vote YES
- All vote YES

1. Draw the truth table for the inputs and output given above and write the SOP expression.
2. Reduce the output using Karnaugh map.
3. Draw the logic gates diagram for the reduced SOP expression.
4. Implement the logic gates diagram for the reduced SOP expression using NAND gate only